## Estimating Derivatives and the Derivative Function.

Numerical
Estimate the derivative at each of the points given below.

| $x$ | 0 | 3 | 6 | 8 | 10 | 11 | 12 | 16 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 100 | $?$ | 70 | $?$ | 55 | $?$ | 46 | $?$ | 40 |
| $f^{\prime}(x)$ |  |  |  |  |  |  |  |  |  |

## Symbolic

For each of the functions below, estimate the derivative at the given point. Show calculations.

$$
f(x)=5^{x} \text {. Estimate } f^{\prime}(2) .
$$

$$
f(x)=x^{3} \text {. Estimate } f^{\prime}(2) .
$$

## Graphical

For each of the graphs below, estimate the derivative at a number of points. Then plot the points.
Can you find a function that gives the slope as a function of $x$ ?
Problem 1


| $\boldsymbol{x}$ | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}^{\prime}(\boldsymbol{x})$ |  |  |  |  |

Problem 2


| $\boldsymbol{x}$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f^{\prime}(x)$ |  |  |  |  |  |  |  |

Problem 3


| $\boldsymbol{x}$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{f}^{\prime}(\boldsymbol{x})$ |  |  |  |  |  |

Problem 4


| $\boldsymbol{x}$ | 0.5 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{f}^{\prime}(\boldsymbol{x})$ |  |  |  |  |  |  |

