

The distance,  $d(t)$  (in light-years) that the starship Enterprise has travelled from Earth after a time,  $t$  (years) is given by

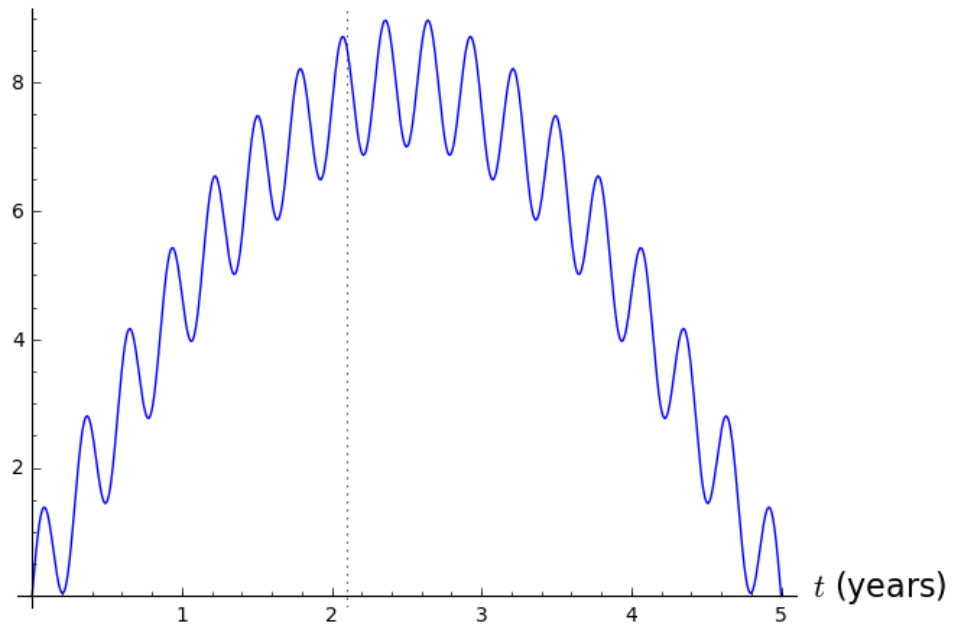
$$8 \sin\left(\frac{\pi}{5}t\right) + \sin(7\pi t)$$

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In [24]: t=var('t')

d(t)=8*sin((pi/5)*t) + sin(7*pi*t)

show(plot( d,t, 0, 5, axes_labels=["t$ (years)","distance$(t)$ (light-years)"], f
igsize=(8,5),
gridlines=[[2.1],[[]]]))
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Out[24]: distance( $t$ ) (light-years)



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In [25]: dp(t)=diff(d(t),t) #This is the derivative of d(t).
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[ n( d(2.1)), n((d(2.1)-d(0))/(2.1-0)), n(dp(2.1)) ]
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Out[25]: [8.55768228340399, 4.07508680162095, -11.6760210973706]
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It would appear that  $d(2.1) = 8.55$ , and  $\frac{d(2.1)-d(0)}{2.1-0} = 4.075$ , and  $d'(2.1) = -11.68$ .

Draw on the graph...

1. The line whose slope represents the **average speed of the Enterprise during the first 2.1 years of its mission.**
2. The line whose slope represents the **instantaneous velocity of the Enterprise 2.1 years after its mission started.**