18. The following table shows revenue, $R$, in hundreds of dollars, at a movie theater as a function of number of tickets sold, $t$, and the number of food items sold, $f$. Thus $R=g(t, f)$.

|  |  | $t$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 100 | 200 | 300 | 400 | 500 |  |  |
| $f$ | 200 | 11 | 19 | 27 | 35 | 43 |  |
|  | 400 | 14 | 22 | 30 | 38 | 46 |  |
|  | 600 | 17 | 25 | 33 | 41 | 49 |  |
|  | 800 | 20 | 28 | 36 | 44 | 52 |  |
| 1000 | 23 | 31 | 39 | 47 | 55 |  |  |
|  |  |  |  |  |  |  |  |

In practical meaning, using everyday words, what is the meaning of $g(200,600)$ ? This is the revenue when 200 tickets and 600 food items are sold
19. The following figure is a contour diagram for the demand for pork as a function of the price of pork and the price of beef? Which axis corresponds to pork and which corresponds to beef? Explain your answer. The $x$ axis is the price of pork and the $y$ axis is the price of beef.


Figure 9.2.284

Could mean:
As the price of beef increases, demand for pork increases.

As $x$ increases (while holding y constant), we cross contour lines of decreasing pork demand. could be:
As the price of pork increases, demand for pork drops.
20. (Multiple Choice) For a certain function $z=f(x, y)$, we know that $f(0,0)=50$ and that $z$ goes up by 3 units for every unit increase in $x$ and $z$ goes down by 2 units for every unit increase in $y$.
What is $\mathrm{f}(2,5) ? z=50+3 x-2 y$. So the answer is $50+3 * 2-2 * 5=46$
(a) 51
(b) 46
(c) 1
(d) 55
(e) -4
(f) 16
21. You build a campfire while up in the mountains. It is $45^{\circ} \mathrm{F}$ when you start the fire. Let $H(x, t)$ be the temperature $x$ feet from the fire $t$ minutes after you start it. The following figure is the contour diagram for $H$.


Figure 9.2.291
(a) How warm is it 8 feet from the fire after 15 minutes?

About 55 degrees
(b) Is $H$ an increasing or decreasing function of $x$ ? of $t$ ? decreasing function of $x$, increasing function of $t$.
22. Sketch a contour diagram of $f(x, y)=2 x-y+1$. Include at least four labeled contours.

Should get a family of straight lines with slope 2 . The contour for $k=1$ should go through the origin. The values of $k$ should decrease vertically.

For the $\mathrm{k}=1$ contour, set $\mathrm{f}=\mathrm{k}=1$ and solve for y:
$1=2 x-y+1$, leads to $y=2 x$
For the $\mathrm{k}=\mathrm{o}$ contour, set $\mathrm{f}=\mathrm{o}$ and solve for y :
 $0=2 x-y+1$, leads to $y=2 x+1$
23. (Multiple Choice) The following table shows values of $f(x, y)$. Does f appear to be an increasing or decreasing function of $x$ ?
Of $y$ ?

|  |  | $y$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0 | 5 | 10 | 15 |
| 3 | 0 | 75 | 72 | 68 | 60 |
|  | 20 | 80 | 77 | 73 | 68 |
|  | 40 | 86 | 82 | 75 | 70 |
|  | 60 | 93 | 88 | 82 | 75 |

Increasing y , while holding x constant at $\mathrm{x}=20$.
(a) Increasing function of $x$; Increasing function of $y$
(b) Increasing function of $x$; Decreasing function of $y$
(c) Decreasing function of $x$; Increasing function of $y$
(d) Decreasing function of $x$; Decreasing function of $y$

Means: if we hold $x$ constant, and only allow $y$ to change, then as y increases, $f(x, y)$ decreases.
5.
24. Which of the graphs (a)-(f) shows a cross section of $f(x, y)=50-x^{2}+5 y$ with $y$ held fixed? Answer is $b$ and $f$.
(a)

(b)

(c)

(d)

(e)

(f)


