

# Math 213 Calculus III

## Reading the Text

Read Section 12.7-12.9 and answer the following questions

1. In the expression  $\int \int \int_E f(x, y, z) dV$ , what does the  $E$  and the  $dV$  mean?
2. What is the solid described by the integral  $\int_{\pi/2}^{\pi} \int_0^{2\pi} \int_0^{\sqrt{3}} \rho^2 \sin \phi \, d\rho \, d\theta \, d\phi$ ?
3. When we convert a double integral from rectangular coordinates to spherical coordinates, where does the  $\rho^2 \sin \phi$  term come from?
4. The *unit square* is the square with side length 1 and lower left corner at the origin. What is the area of the image  $R$  (in the  $xy$  plane) of the unit square  $S$  (in the  $uv$  plane) under the transformation 
$$\begin{aligned} x &= u + 2v \\ y &= -6u - v \end{aligned} \quad ?$$